

$$(b) \quad f(x) = \frac{3x+4}{x^2-49} ; \quad g(x) = \frac{2x-3}{x^2-49}$$

$$\text{Add: } (f+g)(x) = f(x) + g(x)$$

$$= \frac{3x+4}{x^2-49} + \frac{2x-3}{x^2-49}$$

$$= \frac{(3x+4) + (2x-3)}{x^2-49} \quad \leftarrow \text{combine like terms}$$

$$= \frac{5x+1}{x^2-49}$$

$$x^2 - 49 = 0 \\ \sqrt{x^2} = \sqrt{49}$$

$$\text{Domain: } (-\infty, -7) \cup (-7, 7) \cup (7, \infty)$$

$$x \neq \pm 7 \\ x \neq -7 \text{ or } x \neq 7$$

$$\text{Subtract: } (f-g)(x) = f(x) - g(x)$$

$$= \frac{3x+4}{x^2-49} - \frac{2x-3}{x^2-49}$$

$$= \frac{3x+4 - (2x-3)}{x^2-49}$$

$$= \frac{3x+4 - 2x+3}{x^2-49}$$

Same as
addition

$$= \frac{x+7}{x^2-49} = \frac{x+7}{(x+7)(x-7)}$$

$$= \frac{1}{x-7}$$