

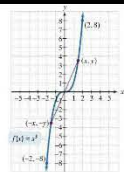
Symmetric with respect to the y-axis

A graph is **symmetric with respect to the y-axis** if, for every point (x, y) on the graph, the point $(-x, y)$ is also on the graph.

- All even functions have graphs with this kind of symmetry.

Even Functions and y-Axis Symmetry

The graph of an even function in which $f(-x) = f(x)$ is symmetric with respect to the y-axis.



Symmetric with respect to the origin

A graph is **symmetric with respect to the origin** if, for every point (x, y) on the graph, the point $(-x, -y)$ is also on the graph.

- All odd functions have graphs with origin symmetry.

Odd Functions and Origin Symmetry

The graph of an odd function in which $f(-x) = -f(x)$ is symmetric with respect to the origin.

Piecewise Function

A function that is defined by two (or more) equations over a specified domain is called a **piecewise function**.

Step Functions

Some piecewise functions are called **step functions** because their graphs form discontinuous steps.

- One such function is called the greatest integer function, symbolized by $\text{int}(x)$ or $\llbracket x \rrbracket$, where $\text{int}(x)$ = the greatest integer that is less than or equal to x .

Example 4: Evaluate the piecewise function at the given values of the independent variable.

$$f(x) = \begin{cases} 4x + 4 & \text{if } x < 0 \\ 4x + 7 & \text{if } x \geq 0 \end{cases} \quad \text{a) } f(-3) \quad \text{b) } f(0) \quad \text{c) } f(1)$$

