

**Equivalent** sets have the same number of elements, or the same cardinality,  $n(A) = n(B)$ .

- A **one-to-one correspondence** between sets A and B means that each element in A can be paired with exactly one element in B, and vice versa,  $n(A) = n(B)$ .
- If two sets can be placed in a one-to-one correspondence, then they are equivalent:  $n(A) = n(B)$ .

**Equal** sets have exactly the same elements, regardless of order or possible repetition of elements. We symbolize the equality of sets A and B using the statement  $A = B$ .

- If two sets are equal, then they must be equivalent.

Example 8: i) Are the sets equivalent? ii) Are the sets equal?

a.  $A = \{9, 10, 11, 12, 13\}$   
 $B = \{8, 9, 10, 11, 12\}$

b.  $A = \{2, 2, 2, 3, 3, 4, 5, 5\}$   
 $B = \{5, 4, 3, 2\}$

c.  $A = \{x \mid x \in \mathbb{R} \text{ and } 12 < x \leq 17\}$   
 $B = \{x \mid x \in \mathbb{R} \text{ and } 20 \leq x < 25\}$

Set A is a **finite set** if  $n(A) = 0$  (that is, A is the empty set) or  $n(A)$  is a natural number.

- A set whose cardinality is not 0 or a natural number is called an **infinite set**.

Example 9: Determine whether each set is finite or infinite.

a.  $\{x \mid x \in \mathbb{R} \text{ and } x \geq 50\}$

b.  $\{x \mid x \in \mathbb{R} \text{ and } x \leq 2,000,000\}$